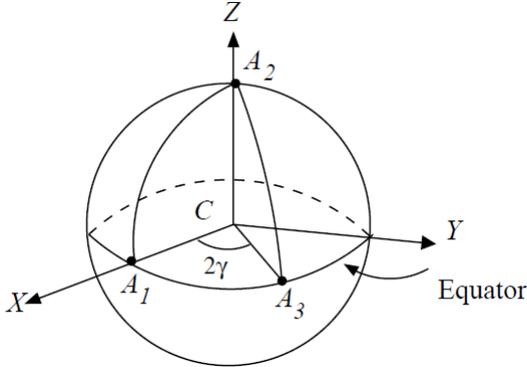




QN	Solution	Marks
III.1	Step 1: Superposition $\delta = \omega \Delta t = \frac{\omega d \sin \theta}{c}$ $ \mathbf{E}_1 + \mathbf{E}_2 ^2 = E_0^2 [\cos^2(\omega t) (1 + 2 \cos \delta + \cos^2 \delta) + \sin^2(\omega t) \sin^2 \delta - 2 \cos(\omega t) (1 + \cos \delta) \sin(\omega t) \sin \delta]$	0.4 0.2
	Step 2: Time averaging: $\overline{\cos^2 \omega t} = \overline{\sin^2 \omega t} = 1/2$ and $\overline{\sin(\omega t) \cos(\omega t)} = 0$,	0.3
	Step 3: Intensity $I(\theta) = \beta \overline{ \mathbf{E}_1 + \mathbf{E}_2 ^2} = \beta E_0^2 (1 + \cos \delta)$	0.1
III.2	The beam 1 has travelled extra optical path = $(\mu - 1) w$.	0.4
	Thus the net phase difference between two beams when they emerge at the angle θ , $\delta = \frac{\omega}{c} (d \sin \theta - (\mu - 1) w)$	0.2
	and $I(\theta) = \beta E_0^2 (1 + \cos \delta)$.	0.4
III.3	The two beams have travelled exactly same paths upto the slits. Thus when they emerge at an angle θ , they have a net phase difference of $\delta = \omega d \sin \theta / c$. Then, notice $ \mathbf{E}_1 + \mathbf{E}_2 ^2 = \left \mathbf{i} \left[\frac{E_0}{\sqrt{2}} \cos(\omega t) + E_0 \cos(\omega t + \delta) \right] + \mathbf{j} \left[\frac{E_0}{\sqrt{2}} \sin(\omega t) \right] \right ^2$	0.70 for x component and 0.3 for y component
	$ \mathbf{E}_1 + \mathbf{E}_2 ^2 = E_0^2 \left[\cos^2(\omega t) \left(\frac{1}{2} + \sqrt{2} \cos \delta + \cos^2 \delta \right) + \sin^2(\omega t) \sin^2 \delta + 2 \cos(\omega t) \left(\frac{1}{\sqrt{2}} + \cos \delta \right) \sin(\omega t) \sin \delta \right] + \frac{E_0^2}{2} \cos^2(\omega t)$	0.3
	Thus, after taking time averages, the intensity will be $I(\theta) = \beta E_0^2 \left[1 + \frac{1}{\sqrt{2}} \cos \left(\frac{\omega d \sin \theta}{c} \right) \right]$	0.3

QN	Solution	Marks
	The minimum value of the intensity is $\beta E_0^2 \left[1 - \frac{1}{\sqrt{2}}\right]$. Maximum value is $\beta E_0^2 \left[1 + \frac{1}{\sqrt{2}}\right]$	0.2+0.2
III.4	The electric field at $z = b$ is given by $\mathbf{E}_1(z = b) = \frac{1}{\sqrt{2}} [E_0 \cos(\omega t - kb - \gamma)] \mathbf{i}'$	magnitude 0.8 , direction 0.2
	The electric field at $z = b$ is given by $\mathbf{E}_1(z = c) = \frac{1}{\sqrt{2}} \cos \gamma E_0 \cos(\omega t - kc - \gamma) \mathbf{i}$	magnitude 0.3, direction 0.2
	Phase difference $\alpha = \gamma$.	0.5
III.5	At equator $e = 0$. Then $\mathbf{E} = \mathbf{E}_{\text{Eq}} = \mathbf{i}' E_0 \cos(\omega t).$ Clearly the beam is linearly polarised along \mathbf{i}' .	\mathbf{E} : 0.2 Linear Polarization: 0.3
III.6	At north pole $e = \pi/4$ and γ can be taken to be 0. Then $\mathbf{i}' = \mathbf{i}$ and $\mathbf{j}' = \mathbf{j}$. The electric field $\mathbf{E} = \mathbf{i} \frac{E_0}{\sqrt{2}} \cos(\omega t) + \mathbf{j} \frac{E_0}{\sqrt{2}} \sin(\omega t)$ or $= \mathbf{i} \frac{E_0}{\sqrt{2}} \cos(\omega t + \gamma) + \mathbf{j} \frac{E_0}{\sqrt{2}} \sin(\omega t + \gamma)$ which represents circular polarisation.	\mathbf{E} : 0.2 Circular Polarization: 0.3
III.7	Figure 	A1 on x axis 0.3, A2 on the north pole 0.5, A3 on equator 0.4, angle of 2γ 0.3
III.8	From figure it is clear that the area of the spherical triangle $A_1A_2A_3$ is $2\pi \times \left(\frac{2\gamma}{2\pi}\right) = 2\gamma$	0.7
	Thus the phase difference α is half the area S of the spherical triangle $A_1A_2A_3$ on Poincaré sphere i.e. $S = 2\alpha$.	0.8